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Continuity

You know that it shouldn't be strenuous
to determine if a function's _____.
'Cause there's a mathematical test you can do
by just checking to see that three details are _____.
For every value in the domain you must first find
if the function at that spot is clearly _____.
Next look closely to see as you near it
whether the function at that point- has a _____.
If to both questions you answer emphatically-YES!
and they're equal, the function is _____.

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Eccentricity!

It's not shocking, like electricity,
that a conic's shaped by it's _____.
For a conic's nothing but a locus
whose ratio is fixed from directrix to _____.
For example, a circle's a shape we all know,
its eccentricity's value's exactly _____.
As the value gets larger, elongating the tips,
the curve that you get is now an _____.
But when e equals one, that oughta tell ya,
the locus you have is now a _____.
As e grows much bigger, it shouldn't perturb ya,
you'll just get a shape we call a _____.

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Function Composition

(A poem which ranges across the cognitive domain)

$$f(x) = \text{I know } x$$

$$f(\text{'functions'}) = \underline{\hspace{2cm}}$$

$$f \circ f(\text{'functions'}) = \underline{\hspace{2cm}}$$

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(Dane R. Camp, Fractal geometry in the high school classroom, International Reviews on Mathematical Education, May, 1995:149)

A Horse of The Same Color.

Induction is easy, so easy to do,
For the steps are the same and there are only _____.

Take a statement that's suspected of being a rule
For the numbers you learned to count with in _____.

First show that some initial case is a fact,
If you can't then the statement you hafta _____.

Then make the wild assumption the statement is true
for some number k , (and all values _____)

If from this you can show that $k + 1$ lurks,
the statement is proved now, and it always _____!

But be careful with induction whatever you do,
For it's easy to slip and make a _____.

For example consider the following "proof"
listen and see if you can locate the _____.

"All horses are the same color" is easily said,
but can they all be brown, black, white or _____?

The basic step quickly goes on the shelf,
For if you have one horse it's the same as _____!

Now assume for any k horses you find,
they're always the same color, no matter the _____.

Consider now, and here it gets fun,
a group of horses numbering _____.

Remove one of the horses, so that there are k ,
"they're all the same color" by the assumption you _____.

Whatever the color they are, it can't change
when we take that one horse and we _____.

The horses again number exactly k ,
So they're all the same color, as before by the _____.

For a horse that remained in the group keeps its
shade, so the color never varies and the proof now is _____.

But there's something wrong, there must be you
know, for this statement is false, at least I think _____.

But where is the error, please tell me will you?
Or I'll go through my life thinking this statement's _____!

"In Verse"

For ANY operation it is plain to see, things
NEVER change if you use the _____.

when you add numbers it should be clear, oh,
nothing changes if you use _____.

and you all know that for multiplicaTION, we've
certainly got to use number _____.

since each domain value it guards and protects,
for function composition it's $f(x)=$ _____.

To undo operations and go in reverse,
you apply something special we call the _____.

anything turns to zero by adding to it,
a number that's special, called it's _____.

and the number one we always reveal,
when multiplying by the _____.

input values for a function come back unchanged
if composed with it's inverse, swapping
_____ and _____.

A function's inverse you often can try,
to find by exchanging the x and the _____.

don't bother to do this, though it may seem fun,
if the original function is not _____.

graphically speaking you can see this best,
for it must first of all pass the _____.

the sketch of an inverse simply reflects,
flipping across the line_____.

(Dane R. Camp, 1997)

Logarithmic Limerick

You'll experience a "powerful" sensation,
By repeating this short incantation:
"The base stays the base,
Switch the terms and replace
The logarithm with exponentiation!

There's a verse which has the same rhythm
about powers, and everything with'm
"The base stays the base,
Switch the terms and just place
in front of it all a logarithm!"

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"Prime Rhyme"

Let's take a few moments to sketch out in rhyme,
exactly what you know when you've got f _____.

For example, when positive, it's visually pleasing,
and the graph of the function is clearly_____.

If it's below zero, like days that are freezing,
the graph of the function must now be_____.

When f prime is zero, the graph seems to tarry,
and the point that you find is called_____.

Yet there's a lot more, as you may have guessed,
a thing called the first derivative_____.

Find a stationary point and consider the facts,
If it goes plus to minus you must have a_____.

If those signs are reversed, it's really no sin,
you've stumbled across a point that's a_____.

And lastly if f' has no change of direction,
the stationary point is a point of_____.

Now if you want to continue to something sublime, consider the
meaning of f'' _____.

If it's positive the function is shaped like a cup
for the slope is increasing and the graph's concave_____.

And negative values will make functions frown, when the slope's
getting smaller the graph's concave_____.

But f'' won't help us to know the concavity if its
value's_____.

See the derivative's power is really not strange for it gives you the
low down on how functions_____.

Prime Rhyme (Part Deux)

So if f' is zero it would be best
to apply the second derivative _____.

If the second derivative's positive it must be grinning,
the concavity's up, so the function is _____.

And if less than zero, it's sure not taxing,
the graphs concave down, so the function is _____.

But if it's equal to zero, we have no direction,
as to max, min, neither, or point of _____.

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$$\frac{P(X)}{Q(X)}$$

P of x over Q of x behaves rationally,
and its secrets are clear if you think carefully.

The zeroes of the denominator tell it's not defined,
if they cancel with the top, then a hole you will find.

But if the factors of the denominator are not cancelled out,
then a vertical asymptote must be lurking about.

Now don't mix those up, or you'll sure pull a gaff,
for you won't know your asymptote from a hole in the graph.

Though the ends of the graph may look somewhat neurotic,
long division reveals that they are really asymptotic.

For the quotient, ignoring the remainder that appears,
will determine the shape that the graph slowly nears.

If the degree of the top's less than that down below,
a horizontal asymptote at the x -axis will show.

If the degrees are the same, the asymptote is still flat,
and the quotient of the coefficients will tell where it's at.

When the numerator's degree exceeds by just one,
the asymptote is oblique on a linear run.

When the discrepancy's bigger, they won't just be slants,
for the asymptotes will do the "polynomial dance!"

The Towers of Hanoi

In a land far away
in a long distant time
the priests in a temple
played a game quite sublime.

With 100 disks
that were set upon
3 stout upright pegs
they played dusk till dawn.

For the priests of Hanoi
knew when the game was done
the whole world would end
and so would their fun.

The rules were quite simple
for there were but two,
and if you listen closely,
I'll share them with you.

The disks could be moved
to pegs one at a time.,
to put larger on smaller
was considered a crime.

There were 100 priests,
who all played this game
they each had one disk
and took turns by name.

The 100th priest
would utter a curse,
for he could not move,
till the others moved first.

So the job was now left to
priest 99,
who also cursed softly,
and took place in line.

And so they all lined up
cursing and recursing,
waiting their turn,
and mentally rehearsing,
their one special move
their own sacred place
in the cosmic scheme
and the human race.

So let us attempt to
act out this drama
for 4 little disks
to lessen the trauma.

And when we are through
with this smaller version,
you will then understand,
what we call recursion.

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The transformation of $f(x)$

If you add to a function you'll give it a lift,
for the graph will be moved with a vertical shift,
But if you multiply take a close look and see,
the graph's stretched by that factor vertically,
and negating the function will cause a reflection,
across the x-axis in an up-down direction.

But if you add before the function's used, hey
The shift's horizontal the opposite way!
And multiplication by a factor inside reveals,
the graph's being stretched by the reciprocal's
And negating the values before f is applied
reflects across the y axis--it flips side to side!

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What is a Radian?

At Baker's Square I crossed my eyes
and every circle became two pies!

It took but a moment to realize,
that to get a central angle's size
divide the arc's length by the radii's!

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When are we ever gonna use this?

When are we gonna use this? Mmmm, let me see...

Perhaps never if you win the state lottery,
Or maybe tomorrow there's a chance that you may,

To be perfectly honest, I really can't say!

For mathematics is a lot like a language and, yes

To predict when you'll use it is anyone's guess.

Just as there are those words that we use all the time

And others that we seldom say, like "sublime,"

There are math skills we happen to use every day,

Like estimating change and computing gross pay,

There are others that have a more specialized function,

Like Trigonometric ratios and 'mathematical induction.

But I can tell you this, if you do your part,

And learn with your head as well as your heart,

You'll solve real problems and comfortably mingle

With the world's greatest minds who are also "bi-lingual,"

And your math fluency will grow through the years,

For you'll know when to use it when the right time

appears.

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Yes!

Yes! Feel the magic
as tingles run up your spine –
trigonometry.

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